

Astro 350  
Lecture 39  
Dec. 7, 2012

Announcements:

- **Homework 11** due now
- Good news: now more homework!
- Bad news: Final Exam next Friday Dec 14, 8-11am here  
www: Final Exam Info online
- **ICES** available online – please do it!  
I do read and use comments!

Last time: cosmic inflation

*Q: what is it? How it is different from (more than) the usual expansion of the universe?*

*Q: how does inflation make the universe flat?*

*Q: how does inflation fix the horizon problem? lumpiness?*

## Inflation

idea: Early U had period of rapid *accelerated* expansion

- during inflation, scale factor grew by  $e^{60} \simeq 10^{26}$ !
- expansion accelerated—like dark energy now

flatness

curvature inflated away [www](#): [balloon analogy](#)

horizon

- ▷ tiny initial causal region ( $\ll$  atom size: microscopic!)
  - ▷ expanded to huge scales ( $\gg$  1 Mpc: macroscopic!)
- diagram: cosmic spacetime with, without inflation*

## density fluctuations

pre-inflation: **microscopic** horizon

→ **quantum** effects important

quantum fluctuations present & *inevitable*

if no expansion, or decelerating expansion

→ fluctuations undone soon after created

but if ***accelerated*** expansion

“nearby” fluctuations soon far apart, carried at speed  $> c$

can't be undone → inflated to macroscopic scales

# Inflation Status

Inflation Scorecard: Fall Semester 2012

Prediction	Score
flatness	★
isotropy	★
fluctuations	★★★★★
gravity waves	DF*

\*Grade deferred till *Planck Explorer: Results public Jan 2013*

## Pessimist's view

- most of these are really post-dictions  
→ inflation *invented* to solve these problems
- no fundamental (i.e., particle physics) understanding of inflaton  $\phi$
- no competing theory as an alternative  
a lack of imagination? a cosmic epicycle?

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*Q: optimist's response?*

## Optimist's view

- fluctuations impressive, and a *prediction*
- turn problem around:  
CMB probes inflation  $\phi$   
 $\Rightarrow$  the U. as the “poor man’s accelerator”
- there *were* competing theories  
for density fluctuation origins, but they’re ruled out now

## Who’s right?

- the data will show (esp. gravity waves)
- but still a good idea to  
try to develop competing ideas...

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## Epilogue: Living With Inflation

Inflation arises from a marriage of

- ideas about unification of forces (inner space)
- ideas about cosmology (outer space)

something like inflation almost unavoidable if combine these

but much remains to be understood

- how did the universe *start* inflating?  
what made vacuum energy dominant?
- how did the universe *stop* inflating?  
what made vacuum energy revert to matter & radiation?

- what if some regions of the universe are still inflating?  
if so, continuously becoming exponentially larger  
→ and our observable universe is a tiny part of the  
mostly inflating cosmic volume
- how are we so lucky to live in a non-inflating region  
sounds very anthropic...

lesson: if true inflation, profoundly changes our view  
of what “the universe” means

# Structure Formation



# Formation of Cosmic Structures

Starting point:

CMB gives a picture of the Universe at  $t = 400,000$  years

- nearly homogeneous

*Q: how would density evolve if  $\delta\rho = 0$  everywhere?*

- but not perfectly: tiny temperature fluctuations present  
 $\Rightarrow$  density *inhomogeneities* present

$$\delta\rho = \rho - \rho_{\text{average}} \neq 0 \quad \text{typically} \quad (1)$$

- CMB: typical density fluctuation size at 400,000 years:

$$(\delta\rho)_{\text{typical,CMB}} \approx \pm 10^{-4} \rho_{\text{average}} \quad (2)$$

- *Q: what does  $\delta\rho < 0$  mean? how often does this occur?*  
*Q: what is  $\delta\rho$  in this room?*

## Density Fluctuations Over Time

at each point in Universe, density fluctuations  $\delta\rho = \rho - \rho_{\text{average}}$  measures *difference* from all-Universe *average density*

- $\delta\rho < 0$ :  $\rho < \rho_{\text{average}}$ , **underdense** (“void”)
- $\delta\rho > 0$ :  $\rho > \rho_{\text{average}}$ , **overdense** (“clump”)

at early times:

$|\delta\rho|_{\text{CMB}} \approx 10^{-4} \rho_{\text{average}}$  – fluctuations *tiny*

today:

average cosmic density  $\rho_{\text{average}} = \rho_{\text{crit}} \approx 10^{-26} \text{ kg/m}^3$

in this room:  $\rho_{\text{room}} \approx \rho_{\text{air}} - \rho_{\text{water}} \approx 1 - 1000 \text{ kg/m}^3$

so  $|\delta\rho|_{\text{room}} \approx (10^{26} - 10^{29}) \rho_{\text{average}}$  – fluctuations *enormous*

*Q: what does this tell us?*

# Cosmic Structure Formation: The Big Picture

The CMB tell us: at  $t = 400,000$  years the Universe was

- nearly homogeneous on all length scales
- with tiny density fluctuations present

Present-day observations tell us: at  $t = 13.6$  billion yrs, U is

- homogeneous on large scales  $\gg 30$  Mpc
- but with huge density fluctuations on smaller scales

Lesson:

- a lot happened between then and now!
- somehow the fluctuations on small scales grew to become large fluctuations = galaxies, stars, people

*Q: so what happened?*

## iClicker Poll: An Overdense Region Over Time

Consider an *overdensity* with  $\rho > \rho_{\text{average}}$   
and thus  $\delta\rho > 0$

Over time, density in the initially overdense region will

- A** become an increasingly higher multiple of the average
  - B** become increasingly closer to the average
  - C** remain the same fraction of the average
- 

12 Q: *what about an underdensity?*  
Q: *what do we conclude about structure formation?*

overdense region:

- more matter → more gravity
  - expands slower → less diluted than average
  - becomes even more dense than average
- runaway process: **gravitational instability**

underdense region: same story but opposite sign

→ runaway process of becoming ever less dense than average

basic outcome:

“the rich get richer and the poor get poorer”

## Seeds of Cosmic Structure

gravity amplifies density fluctuation “seeds”  
(e.g., from inflation)  
grow to structures we see (and are!) today

Challenge:

given  $\delta\rho$  + known cosmic ingredients  
can we understand how we got  
from recombination (“CMB era”) to today?

## A Simplified Inhomogeneous Universe

Consider a stupidly simplistic—but illustrative!—Universe:

- everywhere in space (the average “background”)  
homogeneous: uniform matter density  $\rho_{\text{bg}} = \rho_{\text{crit}}$
- *except* in a sphere  
which has uniform matter density  $\rho > \rho_{\text{crit}}$   
but at first just barely larger, say  $\rho_{\text{init}} = 1.00001\rho_{\text{bg,init}}$   
**“spherical overdensity”**

Cool property of gravity:

behavior of the uniform sphere is *the same*

as an entire universe with same density

i.e., a Universe with  $\rho/\rho_{\text{crit}} = \Omega > 1$

Initially, both the background U and sphere are expanding

*Q: what will happen to the background U? to the sphere?*

*Q: lesson for what happens in an inhomogeneous U?*

background Universe:

has  $\rho = \rho_{\text{crit}}$   $\rightarrow$  evolves like  $\Omega = 1$  Universe

$\rightarrow$  expands forever, density keeps going down

overdense sphere

has  $\rho > \rho_{\text{crit}}$   $\rightarrow$  evolves like  $\Omega > 1$  Universe

- initially expands
- but gravity of sphere slows expansion
- eventually expansion stops, sphere reaches maximum size
- but gravity still attractive: sphere begins to collapse
- continues until reaching high density

lesson: overdense regions initially expand, reach maximum size then “pulls away” from cosmic expansion, and “turn around” collapse to form dense object: (proto) galaxy !?

$\rightarrow$  galaxies formed from overdense “seeds”

$\rightarrow$  also, Brooklyn is not expanding!