The only $\mathbf{2}$ formulas that will be given to you on Exam $\mathbf{3}$ are:

$$
\begin{aligned}
& \mathrm{SD}_{\text {errors }}=\sqrt{1-\mathrm{r}^{2}} * \mathrm{SD}_{\mathrm{y}} \\
& \mathrm{SE}_{\text {slope }}=\frac{\mathrm{SD}_{\text {errors }}}{\sqrt{\mathrm{n} * \mathrm{SD}_{\mathrm{x}}}=\frac{\sqrt{1-\mathrm{r}^{2}}}{\sqrt{\mathrm{n}}} * \frac{\mathrm{SD}_{\mathrm{y}}}{\mathrm{SD}_{\mathrm{x}}}}
\end{aligned}
$$

Formulas you need to know:

- Slope of the regression line $=r \frac{S D_{y}}{S D}$
- Correlation Coefficient, $r=\frac{\sum_{i=1}^{n} Z_{x} Z_{y}}{n}$
- $Z$ and $t$ test stats for testing $H_{0}$ : slope=0 in simple regression (1 slope):

$$
\mathrm{Z}=\frac{\mathrm{r}}{\sqrt{1-\mathrm{r}^{2}}} * \sqrt{\mathrm{n}} \text { and } \mathrm{t}_{(\mathrm{n}-2)}=\frac{\mathrm{r}}{\sqrt{1-\mathrm{r}^{2}}} * \sqrt{\mathrm{n}-2}
$$

- Chi square and $F$ stats for testing $H_{0}$ : All slopes $=0$ in multiple regression

$$
\chi_{(\mathrm{p}-1)}^{2}=\frac{\mathrm{R}^{2}}{1-\mathrm{R}^{2}} * \mathrm{n} \text { and } \mathrm{F}_{(\mathrm{p}-1, \mathrm{n}-\mathrm{p})}=\frac{\mathrm{R}^{2}}{1-\mathrm{R}^{2}} * \frac{\mathrm{n}-\mathrm{p}}{\mathrm{p}-1}
$$

Hint: For simple regression $Z^{2}=\chi^{2}$ and $t^{2}=F$ so just take the square root of the Chi Square and $F$ stats to find the $\mathbf{Z}$ and $t$ stats for simple regression. Remember for simple regression $p=2$ and $R=|r|$.

- ANOVA for regression and means: SST =SSM + SSSE, degrees of freedom: $\mathbf{n - 1}=\mathbf{p - 1}+\mathbf{n} \mathbf{- p}$ $\mathbf{p}=$ \# parameters in your model For regression: $\mathrm{p}=\#$ of $\beta$ 's in regression equation, for means: $\mathbf{p}=\mathbf{g}$ (\# of groups )

| Source | SS (Sum of <br> Squares) | df |
| :--- | :--- | :--- |
| Model | $\mathrm{R}^{2}$ SST <br> SSM (reg) <br> SSB (means) | $\mathrm{p}-1$ <br> $\mathrm{~g}-1$ |
| Error | $\left(1-\mathrm{R}^{2}\right)$ SST SSE <br> (reg) <br> SSW (means) | $\mathrm{n}-\mathrm{p}$ <br> $\mathrm{n}-\mathrm{g}$ |
| Total | SST | $\mathrm{n}-1$ |

## Exam 3 Study Guide

## Part VIII Chapter 21 (pages 107-111)

Question 1: 717 Stat 100 students rated their belief in the existence of ghosts on a scale of 1-10 ( 1 is certain ghosts don't exist and 10 is certain they do exist). They also classified their hometowns into 4 types: Small Town, Medium City, Suburb, and Big City.
Here are the results:

|  | Level of hometown | Average | SD | n |
| :--- | :---: | :---: | :---: | :---: |
| Ghosts | small_town | 4.769 | 3.096 | 121 |
| Ghosts | medium_city | 4.115 | 2.833 | 104 |
| Ghosts | suburb | 5.140 | 3.106 | 356 |
| Ghosts | big_city | 5.309 | 3.064 | 136 |

a) What's the appropriate significance test the null that all 4 group means are the SAME in the "population". We just happen to see small differences in our sample due to chance?
i)
$Z$ test only ii) t test only
iii) F-test only
iv) either $\mathrm{z}, \mathrm{t}$ or F
v) either $t$ or $F$
b) What's the alternative hypothesis
i) All 4 group means are different than each other in the population.
ii) Some group means are different than each other in the population.
iii) One of the group means is different than the others in the population.
iv) That either i , ii, or iii is true.

Fill out the ANOVA table below to test the null hypothesis that all the group means are the same in the population we just happen to see differences in the sample due to sampling variation. Show work inside each box (except for the df column). Write your answers in the blanks provided.


## Exam 3 Study Guide

Part IX Simple Regression: Chapters 23-25
Question 2 pertains to the 4 scatter plots below:


Write the letter of the plot next to the correlation coefficient that is closest to it.
a) $\mathrm{r}=0.36$ $\qquad$ b) $\mathrm{r}=0.9$ $\qquad$ c) $\mathrm{r}=-0.79$ $\qquad$ d) $\mathrm{r}=-0.46$ $\qquad$

Question 3
Compute the correlation coefficient ( $\mathbf{r}$ ) between X and Y by filling in the table below. Plot the points on the graph and check that the plot and r agree.

| X | Y | X in Standard Units | Y in Standard Units | Products |
| :---: | :---: | :---: | :---: | :---: |
| 2 | 4 |  |  |  |
| 4 | 6 |  |  |  |
| 5 | 5 | 0 |  |  |
| 6 | 2 | 0.5 |  |  |
| 8 | 8 |  |  |  |

a) The correlation coefficient, $\mathrm{r}=$ $\qquad$

b) Using the result of part (a), determine the correlation coefficient for each of the following data sets. No computation is necessary. Write your answers in the blanks provided. Your answer should be a number.

| $x$ | $y$ | $x$ | $y$ | $x$ | $y$ | $x$ | $y$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | -8 | 8 | 8 | 4 | 4 | 4 | 2 |
| 4 | -12 | 5 | 5 | 6 | 6 | 6 | 4 |
| 5 | -10 | 2 | 4 | 7 | 5 | 5 | 5 |
| 6 | -4 | 4 | 6 | 8 | 2 | 2 | 6 |
| 8 | -16 | 6 | 2 | 10 | 8 | 8 | 8 |
|  |  | $r=$ |  | $r=$ |  | $r=$ |  |

## Exam 3 Study Guide

Question 4 pertains to the scatter plot below that shows the midterm and final exam scores for 107 students.
Final score


|  | Average | SD |
| :--- | :---: | :---: |
| Midterm | 83 | 9 |
| Final | 74 | 10 |

Correlation: $r=0.6$
a) Which is the regression line?

Choose one:
i) Line 1
ii) Line 2
b) Look at students A, B, C and D on the graph. How did their actual scores on the final compare to their predicted scores?

For each student circle whether their actual final exam scores were better than, worse than, or the same as the regression line predicted from their midterm scores.

|  | Actual Final Scores Compared to Predicted Ones |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Student $A$ | Choose One: | Better | Worse | The Same |
| Student $B$ | Choose One: | Better | Worse | The Same |
| Student C | Choose One: | Better | Worse | The Same |
| Student D | Choose One: | Better | Worse | The Same |

c) Without any information about a particular student's midterm score, what would you expect him to score on the Final?
d) About $68 \%$ of the time, your prediction in part (c) will be correct to within $\qquad$ points.
e) Suppose you are told that the student has a midterm score of 74 . Now what would you predict for his score on the final exam? Use the 3 step process (not the regression equation) Show your work! Circle answer.
f) About $68 \%$ of the time, your prediction in part (e) will be correct to within $\qquad$ points. Show your work!
g) If a student was exactly average on both the midterm and the final which line would he fall on?

Choose one: Only the SD Line Only the Regression Line Both Neither
h) If a student was exactly1 SD above average on both the midterm and the final which line would he fall on?

Choose one: Only the SD Line Only the Regression Line Both Neither
i) If a new scatter plot was drawn with 10 pts. added to everyone's final score then the correlation between midterm and final scores would.... Choose one: i) increase ii) decrease iii) stay the same (For (i) and (j) assume that final scores are allowed to exceed 100)
j) If a new scatter plot was drawn with $10 \%$ added to everyone's final score then the correlation between midterm and final scores would___ Choose one: i) stay the same ii) decrease iii) increase
h)

If point $A$ was removed the, $r$ would ... i) Decrease ii) Increase
iii) Stay the Same

## Exam 3 Study Guide

Question 5 The following scatter plots show the relation between poverty level (percentage of people living below the poverty line) and number of doctors (per 100,000 people) by state and by geographical region. The graph on the left has 50 points, one for each individual state's poverty and doctor level. The graph on the right has the same information condensed into 9 points, one for each of the 9 geographical regions. (In other words, the 50 states were divided into 9 geographical regions. The average poverty and doctor level was computed for each region.)

## By State

## By Division



a) The correlation coefficient for the graph on the left is -0.2 . The correlation for the graph on the right is closest to
i) -0.2
ii) -0.6
iii) 0
iv) 0.2
v) 0.6
b) The scatter plots above are an illustration of
i) The Regression Effect
ii) Simpson’s Paradox
iii) Ecological Correlation
iv)Negative Correlation

Question 6 For each of the following pairs of variables, check the box under the column heading that best describes its correlation among typical STAT 100 students:

| Correlation | Exactly | Between | About | Between | Exactly |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | -1 | -1 and 0 | 0 | 0 and 1 | +1 |

a) Weight in lbs.
Weight in kilograms
(There are $2.2 \mathrm{lbs} . / \mathrm{kg}$ )
b) Weight in lbs.
GPA
c) Freshman GPA Sophomore GPA
d) How much you fall
How much sleep you got asleep in class the night before
Number of Points
Number of points missed
e) scored on Exam 1 on Exam 1

## Exam 3 Study Guide

## Question 7

Here are the (rounded) summary statistics for height and weight of the 325 men in our class who completed Survey 1.

|  | Average | SD |
| :--- | :---: | :---: |
| Height | $71 "$ | $3 "$ |
| Weight | 175 lbs. | 30 lbs. |

Correlation: $r=0.5$
a) One student is exactly one SD above average in height and falls on the regression line. How many lbs. does he weigh?
b) Another student is $65^{\prime \prime}$ tall, predict how many lbs he weighs. Show work. Circle answer.
c) What is the RMSE when predicting weight from height? Show work. Circle answer. Round your answer to the nearest lb.
d) If a student is 71 " and weighs 175 lbs . he would fall on the $\ldots$.

## Choose one:

i) SD line only
ii) regression line only
iii) Neither
iv) Both
e) What is the slope for predicting weight from height?

Show work, circle answer.
f) The men in our class who are 68 " weigh 160 lbs . on the average. Can you conclude that the men in our class who weigh 160 lbs . are 68 " tall on the average?

## Choose one:

i) Yes
ii) No, they'd be taller than $68^{\prime \prime}$ on the average.
iii) No, they'd be shorter than 68 " on the average.
g) The regression equation for predicting height from weight is : Height $=\mathbf{. 0 5} \mathbf{i n c h} / \mathbf{l b} *($ Weight $)+$ $\qquad$ Find the y-intercept. Show work, write answer in blank below. Give your answer to 2 decimal places.
h) If all the heights of the men were converted to centimeters (by multiplying each height by $2.54 \mathrm{~cm} / \mathrm{inch}$ ) the correlation coefficient would ...
Choose one: i) increase
ii) decrease
iii) stay the same
iv) not enough information given

## Exam 3 Study Guide

## Part X: Inference for Regression: Chapters 26-29

## Question 8 Part I

The scatter plot below depicts the height and shoe size of 100 UI male undergrads


|  | Avg | SD |
| :--- | :---: | :---: |
| Height | $71 "$ | $3 "$ |
| Shoe Size | 11 | 1.5 |$r=0.7$


| Shoe Size | 11 | 1.5 |
| :--- | :--- | :--- |

a) Find the slope and $y$-intercept of the regression equation for predicting shoe size from height.

Shoe Size = $\qquad$ Height + $\qquad$ (Round to 2 decimal places.)
b) What is the $\mathrm{SD}_{\text {errors }}$ for predicting shoe size from height?
i) 3
ii) 1.5
iii) 0.51
iv) 0.71
v) 1.07
vi) 2.14

Question 8 part II deals with inference - using the sample slope to make inferences about the population slope.
Now suppose the 100 students from Question 7 were randomly chosen from all male UI undergrads.
a) This corresponds to drawing $\qquad$ points, at random $\qquad$ replacement from a scatter plot depicting (write a number in the first blank and "with" or "without" in the second blank)
i) the heights and shoe sizes of all male UI undergrads
ii) the heights and shoe sizes of the 100 randomly drawn students
iii) the heights and shoe sizes of all UI undergrads
b) Our best estimate of the slope for the whole population = $\qquad$ with a $\mathrm{SE}=$ $\qquad$ -.
Show work for SE. Round to 3 decimal places. You don't need to re-calculate the sample slope.
c) Find the following confidence intervals for the slope of all UI undergrads when predicting shoe size from height. (Round answers to 3 decimal places.) Use the Normal Curve.

90\% Confidence Interval = $\qquad$ +/- $\qquad$ $\mathrm{SE}_{\text {slope }}=$ $\qquad$ to $\qquad$
95\% Confidence Interval = $\qquad$ +/- $\qquad$ $\mathrm{SE}_{\text {slope }}=$ $\qquad$ to $\qquad$
d) In part (c) above we saw that a $90 \%$ confidence interval for slope did not include 0 .

Based only on that information, you could conclude that a Z test for slope would $\qquad$ the null hypothesis that slope $_{\text {pop }}=0$ against the alternative that slope $\qquad$ 0 at $\alpha=10 \%$.

Fill in the $1^{\text {st }}$ blank with "reject" or "not reject" and the $2^{\text {nd }}$ with " $>$ " or " $\neq$ ".
(Hint: 90\% CI interval has 5\% area in each tail.)

Question 8 Part III: Z and $t$ tests for Slope in Simple Regression Formulas you'll need to know. (Or derive them from the $\mathbf{2}$ formulas you're given.)

$$
\mathrm{Z}_{\text {slope }}=\frac{\text { obs slope }-\exp \text { slope }}{\mathrm{SE}_{\text {slope }}}=\sqrt{\mathrm{n}} \frac{\mathrm{r}}{\sqrt{1-\mathrm{r}^{2}}} \quad \mathrm{t}_{\text {slope }}=\frac{\text { obs slope }-\exp \text { slope }}{\mathrm{SE}_{\text {slope }}^{+}}=\sqrt{\mathrm{n}-2} \frac{\mathrm{r}}{\sqrt{1-\mathrm{r}^{2}}}
$$

a) Compute the Z statistic to test $\quad \mathbf{H}_{\mathbf{0}}:$ slope $_{\text {pop }}=\mathbf{0} \quad \mathbf{H}_{\mathrm{a}}:$ slope $_{\text {pop }}>\mathbf{0}$
b) To change the Z -stat above to a t-statistic you would multiply by $\qquad$ .
i) $\sqrt{\frac{98}{100}}$
ii) $\sqrt{\frac{100}{98}}$
iii) $\frac{100}{98}$
iv) $\frac{98}{100}$
v) $\sqrt{\frac{99}{100}}$
vi) $\sqrt{\frac{100}{99}}$
c) How many degrees of freedom does the t -test have? $\qquad$
d) How do p -values for Z and t tests compare when performed on the same data sets with the same null and alternative hypotheses?
i) Z tests will always yield smaller p -values
ii) Z tests will always yield larger p -values
iii) Both tests will yield exactly the same p-values
iv) Depending on the sample size the p -values from the z test could be larger, smaller or the same as the corresponding p -values from the t -test.

## Exam 3 Study Guide

## Question 9

The scatter plot below depicts the body temperatures and heart rates (beats per minute) of 130 adults. Pretend the 130 people were chosen randomly from all Illinois adults.



Sample Regression Equation
Heart Rate $=-171+2.5$ (Temperature)
a)What is the SE of the sample slope? Show work and round your answer to 2 decimal places.
b) A $95 \%$ confidence interval for the population slope using the Normal Curve is ( $\qquad$ to $\qquad$ ).

Round your answers to 2 decimal places.
c) The confidence interval above didn't include 0 , so if we did a 2 sided $Z$ test, testing the null hypothesis that the slope $=0$ for the whole population we should $\qquad$ the null. Reject? or Not Reject? Circle one.
d) Do the hypothesis test by calculating Z and the p -value. The null and alternative are:
$\mathbf{H}_{0}$ : Slope of the regression equation for the whole population is 0 . We just happened to get a small slope of $\mathbf{2 . 5}$ in our sample of $\mathrm{n}=130$ due to the luck of the draw.
$\mathbf{H}_{\mathrm{a}}$ : Slope of the regression equation for the whole population $\neq 0$. Our sample slope of $\mathbf{2 . 5}$ is too big to be due to chance variation.
i) Calculate the test statistic Z for the slope.
ii) Mark $Z$ on the Normal Curve and find $p$-value.
iii) Conclusion? Reject null?


## Exam 3 Study Guide

## Question 10

We're trying to fit a simple linear regression model for the whole population: $\mathrm{Y}=\beta_{0}+\beta_{1} \mathrm{X}+\varepsilon$. (Assume $\varepsilon$ are independent and normally distributed with constant variance). We draw a random sample of $\mathbf{n}=\mathbf{7}$ from the population and get a sample correlation $\mathbf{r}=\mathbf{0 . 6}$. Compute the 4 test statistics for testing the null $\mathbf{H}_{0}: \boldsymbol{\beta}_{\mathbf{1}}=\mathbf{0}$. (same as testing $\mathbf{H}_{0}: \mathbf{r}_{\text {population }}=\mathbf{0}$.) (Round your final answers to 4 decimal places, but don't round during intermediate steps.)
a) $\mathbf{R}^{2}=$ $\qquad$ $1-R^{2}=$ $\qquad$
b) Now compute the 4 statistics below.

c) Compute the p -values for each statistic. Assume the alternative for the Z and t test is 1 -sided:
$\mathbf{H}_{\mathrm{A}}: \boldsymbol{\beta}_{\mathbf{1}}>\mathbf{0}$, and assume the alternative for the $\chi^{2}$ and F is 2-sided: $\mathbf{H}_{\mathrm{A}}: \boldsymbol{\beta}_{\mathbf{1}} \neq \mathbf{0}$.

*If Z is between 2 lines on the Normal Table you may approximate middle area.
d) Suppose our sample y values are: $1,2,3,4,5,6,7$. Compute the SST. (Show work).
e) Compute SSM. $\qquad$ Hint: Use part (a)

## Exam 3 Study Guide

Part X1: Binary Variables in a Regression Model (Chapter 30)

## Question 11

Here's a scatter plot of the heights and weights of the 227 males and 485 females who responded to Survey 1 in Spring 2012.


| Equation | $\mathbf{r}$ | SD $_{\text {errors }}$ |
| :---: | :---: | :---: |
| Weight $=-190.8+5.061 \times$ Height | 0.6149 | 25.84 |

a) Why is $r(0.6149)$ larger in the combined male female plot to the left than in the 2 separate regression below?
Circle all that are true.
i) Because there are more points in the combined plot
ii) Because males are both taller and heavier on the average so combining males and females in one plot increases r .
iii) Whenever two positively correlated groups are combined the correlation increases.
b) Here's the scatter plot broken into groups fitted with the same slope


Fill in the blanks in the equations below to match the equations for males and females above.
(Hint: Males are coded 0, so fit the equation to males first by subbing in 0 for Gender)
Weight $=$ $\qquad$ $+$ $\qquad$ Hgt + $\qquad$ Gender

## Exam 3 Study Guide

## Chapter 37

Question 12 There are 3 sections to the MCAT: Physical Science (PS); Biological Science (BS); and Verbal Reasoning (VR). Each is scored on a scale of 1-15. Suppose we randomly selected 55 UI pre-meds from all UI premeds who took the MCAT last year and got the following sample multiple regression equation for predicting PS
from both VR and BS: $\hat{\mathrm{PS}}=1.6+0.2 \times \mathrm{VR}+0.6 \times \mathrm{BS}$
Summary Stats

|  | Average | Median | SD | Min | Max | $n$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| VR | 9.764 | 10.00 | 1.768 | 6.000 | 13.00 | 55.00 |
| BS | 9.782 | 10.00 | 1.522 | 6.000 | 14.00 | 55.00 |
| PS | 9.709 | 10.00 | 1.659 | 5.000 | 14.00 | 55.00 |

a) Here's the ANOVA table to test the overall regression effect. Fill in them missing values. You'll need to use some info from the summary stats above to calculate SST.

| Source | SS (Round to nearest <br> whole number) | df | MS (Round to 1 <br> decimal place) | (Round to 2 decimal places) |
| :--- | :--- | :--- | :--- | :--- |
| Model | SSM= 63 |  |  | $\mathrm{F}=$ |
| Error | SSE= |  |  | $\mathrm{SD}_{\text {errors }}^{+}=$ |
| Total | SST $=$ |  | $\mathrm{R}^{2}=$ |  |

b) Our F is $>$ or $<\mathrm{F}^{*}=$ $\qquad$ so our p-value > or < $\qquad$ \% so we can or cannot reject the null.
Circle the correct " $>$ " or " $<$ " signs, fill in the 2 blanks and circle "can" or "cannot"
$F$ Distribution critical values for $P=0.001$

| $₹$ Denominator |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Numerator DF |  |  |  |  |  |  |  |  |  |  |  |  |  |
| DF | 1 | 2 | 3 | 4 | 5 | 7 | 10 | 15 | 20 | 30 | 60 | 120 | 500 | 1000 |
| 1 | 405284 | 499999 | 540379 | 562500 | 576405 | 592873 | 605621 | 615764 | 620908 | 626099 | 631337 | 633972 | 635983 | 636301 |
| 2 | 998.50 | 999.00 | 999.17 | 999.25 | 999.30 | 999.36 | 999.40 | 999.43 | 999.45 | 999.47 | 999.48 | 999.49 | 999.50 | 999.50 |
| 3 | 167.03 | 148.50 | 141.11 | 137.10 | 134.58 | 131.58 | 129.25 | 127.37 | 126.42 | 125.45 | 124.47 | 123.97 | 123.59 | 123.53 |
| 4 | 74.137 | 61.245 | 56.177 | 53.436 | 51.712 | 49.658 | 48.053 | 46.761 | 46.100 | 45.429 | 44.746 | 44.400 | 44.135 | 44.093 |
| 5 | 47.181 | 37.122 | 33.202 | 31.085 | 29.752 | 28.163 | 26.917 | 25.911 | 25.395 | 24.869 | 24.333 | 24.061 | 23.852 | 23.819 |
| 7 | 29.245 | 21.689 | 18.772 | 17.198 | 16.206 | 15.019 | 14.083 | 13.324 | 12.932 | 12.530 | 12.119 | 11.909 | 11.747 | 11.722 |
| 10 | 21.040 | 14.905 | 12.553 | 11.283 | 10.481 | 9.5174 | 8.7539 | 8.1288 | 7.8038 | 7.4688 | 7.1224 | 6.9443 | 6.8065 | 6.7846 |
| 15 | 16.587 | 11.339 | 9.3352 | 8.2526 | 7.5673 | 6.7408 | 6.0808 | 5.5351 | 5.2484 | 4.9502 | 4.6378 | 4.4749 | 4.3478 | 4.3275 |
| 20 | 14.819 | 9.9526 | 8.0984 | 7.0960 | 6.4606 | 5.6920 | 5.0753 | 4.5618 | 4.2900 | 4.0051 | 3.7030 | 3.5439 | 3.4184 | 3.3981 |
| 30 | 13.293 | 8.7734 | 7.0544 | 6.1245 | 5.5339 | 4.8173 | 4.2389 | 3.7528 | 3.4928 | 3.2171 | 2.9197 | 2.7595 | 2.6310 | 2.6100 |
| 60 | 11.973 | 7.7678 | 6.1712 | 5.3067 | 4.7565 | 4.0864 | 3.5415 | 3.0781 | 2.8265 | 2.5549 | 2.2522 | 2.0821 | 1.9390 | 1.9150 |
| 120 | 11.380 | 7.3212 | 5.7814 | 4.9471 | 4.4157 | 3.7669 | 3.2372 | 2.7833 | 2.5345 | 2.2621 | 1.9502 | 1.7668 | 1.6027 | 1.5736 |

c) When the null is true we'd expect our $F$ to be about $\qquad$ Given how your F compares to that you'd expect the p -value to be about $\qquad$ $\%$.
d) Suppose you decided to reject the null, you'd conclude that
i. Both slopes must be significant
ii. The VR slope must be significant
iii. The BS slope must be significant
iv. The intercept must be significant
v. Either the VR or the BS slope or both must be significant

## Exam 3 Study Guide

## Question 13

On a Stat 100 Survey, 764 students reported how many drinks they typically consumed per week, how many hours they typically exercised per week and their GPA. The multiple regression equation predicting GPA from drinks and exercise yielded $\mathrm{R}=0.04$. Assume these students were randomly sampled from a larger population of possible Stat 100 students.
a) Do a $\chi^{2}$ test for the overall regression effect. How many degrees of freedom? $\qquad$
b) Compute the F stat. How many df in the numerator $\qquad$ ? The denominator $\qquad$ ?
c) Here are the p -values for the 2 tests. Which one is for the $\chi^{2}$ and which is for the F ? $55.74 \%$ and $55.58 \%$ Label each as either $\chi^{2}$ or F .

## Question 13

In the overall regression test, the null hypothesis is that the population slopes all $=0$.
That's equivalent to the null hypothesis that in the population ....
i) $\quad \mathrm{R}=0$
ii) $\quad R^{2}=0$
iii) $\quad \mathrm{Y}=\overline{\mathrm{Y}}$
iv) all of the above
v) none of the above

## Question 14

If the $\chi^{2}$ test doesn't yield significant results, is it possible the F test still would?
i) Yes, since the F test yields slightly more precise tests.
ii) Yes, if the sample size is relatively small, the F test results could yield significantly different results.
iii) No, the p -value for the F test will always be greater so it could never yield more significant results.
iv) It's impossible to know since $F$ is centered at 1 when the null is true and the $\chi^{2}$ is centered at its degrees of freedom making comparisons of results statistically meaningless.

