

Astro 210
Lecture 16
Feb 25, 2011

Announcements

- HW4 due
- HW5 available, due in one week
- Night Observing: try again next week – *Dress warmly!*
report forms, info online

The Solar System

The Solar System

www: Place in the Big Picture

Why study the Solar System?

- ▷ it's home!
- ▷ use present to learn about past
 - clues for origins of Earth & Sun
- ▷ help understand origin of exoplanets: compare/contrast

Sociology: traditionally, astronomy divided into study of solar system vs extrasolar objects

boundary is artificial, and somewhat loosening now...

Basic Organization www: SS lineup

Terrestrial planets (Earth-like): smaller, rocky
Mercury, Venus, Earth/Moon, Mars

Asteroid Belt: rocky debris

Jovian planets (Jupiter-like): large, gaseous
Jupiter, Saturn, Uranus, Neptune

Kuiper Belt & Oort Cloud: Icy debris

Pluto: in summer 2006, demoted to “dwarf planet”

↳ → will discuss what’s behind this

Patterns in Planetary Orbital Dynamics

all planets & asteroids:

- move in same direction
- close to ecliptic plane
...except Pluto
- note also that *most orbits almost circular*
biggest exception is Pluto

But could it have been otherwise?

Q: What rules does Newton impose on bound orbits?

And note the near-circularity of orbits:

consider a planet at initial distance \vec{r}_{init}

and release it with velocity \vec{v}_{init}

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Q: how does orbit depend on \vec{v}_{init} magnitude, direction?

*Q: how to adjust \vec{v} to get a *circular* orbit?*

Newton/Kepler Motion and Initial Conditions

Given:

- initial position \vec{r}_{init} , and
- velocity \vec{v}_{init}

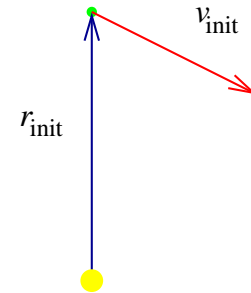
trajectory (orbit) completely determined by Newton's laws

- if $v_{\text{init}} \geq v_{\text{esc}}$, orbit is *unbound*
→ leaves solar system on parabolic or hyperbolic orbit
- for $v_{\text{init}} < v_{\text{esc}}$, a *bound* orbit: ellipse or circle...but which one?

iClicker Poll: Orbits and Initial Conditions

What if bound orbit where \vec{v}_{init} has *nonzero* component along \vec{r}_{init} ?

Q: what kind of orbit will this be?



A ellipse ($e > 0$)

B circle ($e = 0$)

C either ellipse or circle, depending on size of v_{init} at r_{init}

The Miracle of Circular Orbits

- for $v_{\text{init}} < v_{\text{esc}}$, a *bound* orbit

if \vec{v}_{init} has *any* component along \vec{r}_{init}
velocity is *not purely tangential*

i.e., failure to meet circular requirement $\vec{v}_{\text{circ}} \perp \vec{r}$
 \Rightarrow orbit *must* be an **ellipse**

but even if $\vec{v}_{\text{init}} \perp \vec{r}_{\text{init}}$, circle not guaranteed

if $v_{\text{init}} \neq v_{\text{circ}} = \sqrt{GM/r_{\text{init}}}$, orbit *must* be an **ellipse**

circular orbits result *only if* $\vec{v}_{\text{init}} \perp \vec{r}_{\text{init}}$ *and* $v_{\text{init}} = v_{\text{circ}}$ *exactly!*

Lesson: ellipse is “generic” bound orbit

∞ circular orbits are “fine tuned” and special

\Rightarrow **the near-circularity of planet orbits cries out for explanation!**

Planet Properties

Collected here for reference; discussion follows

Note trends, distinctions between terrestrial/Jovian

Property	Terrestrial	Jovian	Pluto
Members	Merc, Ven, Earth/Moon, Mars	Jup, Sat, Urn, Nep	PL
avg dist. from Sun (a)	0.4 – 1.5 AU	5.2 – 30 AU	39 AU
size R	\sim earth	4–11 earth	\sim 0.2 earth
mass	\lesssim earth	15–300 earth	\sim 0.002 earth
density	3000–5000 kg/m ³	\sim 1000 kg/m ³	\sim 2000kg/m ³
interior	rocks, metals	gas, ice, metal core	?
spin period	\gtrsim 1 day	\lesssim 1 day	6 days
atmosphere	none, CO ₂ , O ₂ , N ₂	H ₂ , He, H-compounds	methane CH ₄

Composition

composition = what mix of elements

note: density \leftrightarrow composition connection

density: mass/volume ratio M/V

for solids & liquids: denser \rightarrow richer in heavy elements

e.g., water (H_2O): $\rho = 1000 \text{ kg/m}^3$

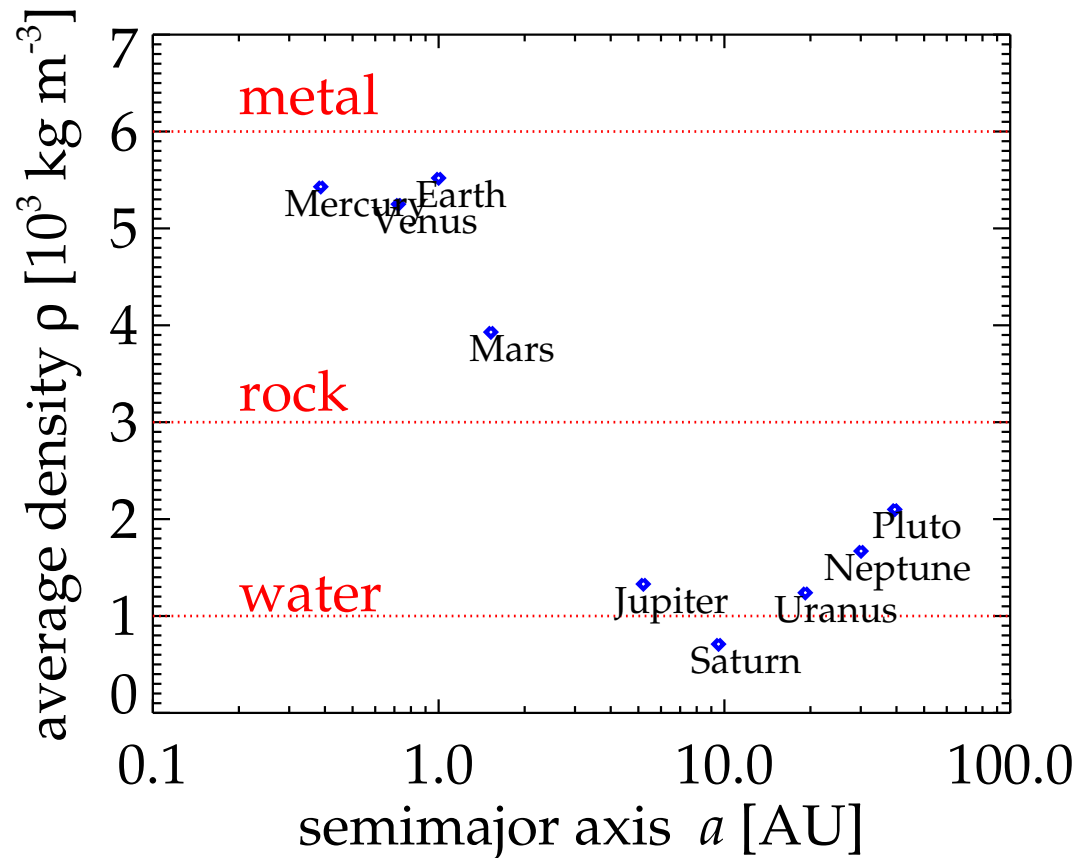
rocks (O,Si): $\rho \sim 3000 \text{ kg/m}^3$

metals (Ni,Fe): $\rho \sim 6000 \text{ kg/m}^3$

for planets, once mass M and radius R are known Q : *how?*
can compute *average* density

$$\langle \rho \rangle = \frac{M}{V} = \frac{3M}{4\pi R^3} \quad (1)$$

Average Planetary Density



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Q: what trends do you notice?

Q: what does this teach us?

Q: what are limitations of this comparison?

Planet Spins

Observed spins: general trends

almost all planet spin in roughly same direction as orbit
i.e., angle (“obliquity”) between spin and orbit axes is *small*
and so spin angular momentum vectors \vec{J}
typically roughly aligned with orbit angular momentum \vec{L}

i.e.: $\uparrow_{\text{orbit}} \uparrow_{\text{spin}}$

→ another highly organized pattern demanding explanation

note: important exceptions do exist

- Venus: spin is retrograde (“upside-down”) $\uparrow_{\text{orbit}} \downarrow_{\text{spin}}$
- Uranus: sideways $\uparrow_{\text{orbit}} \rightarrow_{\text{spin}}$

www: planetary obliquities

→ these too needs to be understood

Surface Temperature

Measuring Temperatures

Q: How to measure planet surface temperatures?

...before visiting! have plan ahead to decide on wardrobe!

hint—*not* Wien's law in simpleminded way! (consider blue Earth!)

Q: expectations from trends of T vs distance d from Sun?

iClicker Poll: Temperature and Planet Size

Consider two planets both at same distance d from Sun and identical (same composition, etc), *except* planet Huge is larger than planet Tiny: $R_{\text{Huge}} > R_{\text{Tiny}}$

Vote your conscience:

Which planet is hotter?

A

planet Huge

B

planet Tiny

C

they have the same temperature

Measuring Temperatures

key point: the visible light that lets you see the planet

is not blackbody emission → reflected sunlight

but: there *is* black body emission at longer λ : infrared

www: IR Moon, Mars

General trends:

indeed, T drops with distance d

but less strongly than $1/d$ (*not* an inverse square law for T !)

we would like to (and can!) understand in detail

Understanding Temperatures

Q: *what are sources of heating? of cooling?*

Q: *what physical laws/conservation principles are important?*

Q: *what sets planetary surface temperatures?*

The Astrophysics of Planetary Temperatures

- ▷ surface heating dominated by radiation ‘
(i.e., energy flow) from the Sun’s emission, peaked at optical λ
“geo” thermal (usually) small contribution (but large for Jupiter)
- ▷ cooling also due radiation (blackbody emission, peaked at IR)

Note: Sun is steady source of light

i.e., constant luminosity = power = Wattage = L_{\odot}

each planet constantly receives this radiation

and also emits its own, according to its T

★ planet $T \rightarrow$ constant value (in time),

★ set by an **equilibrium**:

incoming/outgoing energy flows exactly balance!

Q: *Why? What would happen if inflow > outflow? vice versa?*

planetary energy flows (i.e., power or wattage W):

- W_{in} = absorbed sunlight energy: constant power flow in
- W_{out} = blackbody emission:
strong increasing function of T

What if $W_{\text{out}} > W_{\text{in}}$?

energy conservation \rightarrow planet has net energy loss

\rightarrow suffers **cooling** \rightarrow reduces W_{out}

if new $W_{\text{out}} > W_{\text{in}}$? still, then lather, rinse, repeat

until $W_{\text{out}} = W_{\text{in}}$! equilibrium achieved!

What if $W_{\text{out}} < W_{\text{in}}$?

can convince yourself: planet **warms** until $W_{\text{out}} = W_{\text{in}}$!

equilibrium achieved in this case too!

lesson: all roads lead to equilibrium!

- ∇ If Sun's emission steady, then planet T must go to steady value, set by energy-conserving balance:

$$W_{\text{out}} = W_{\text{in}}$$

Planetary Temperatures Calculated

Can get excellent estimate of planetary T from (fairly) simple first-principles calculation!

key is energy (power) balance: absorption = emission
diagram: sun, planet. label R_{\odot} , d , R

Absorption

recall: if surface of area S_{surf} emit flux F_{surf}

then radiated power = luminosity [energy/sec] is $L = F_{\text{surf}} S_{\text{surf}}$

Sun: $L_{\odot} = F_{\odot} S_{\odot} = 4\pi R_{\odot}^2 \sigma T_{\odot}^4$

at planet, flux is $F = L / 4\pi d^2 = \sigma T_{\odot}^4 (R_{\odot} / d)^2$ [energy/area/sec]

....but we know not all incoming sunlight is absorbed!

Q: *Why not?*

Q: *What substance would absorb all incident sunlight?*

Q: *What substance would absorb no incident sunlight?*

Q *how could we simply quantify all of this?*