

Astro 210  
Lecture 35  
April 20, 2011

### Announcements

- HW 10 due next time: computer-based, pick one of two  
for the theory-inclined: simulate a star  
for the observation-inclined: cosmology data analysis
- also due Friday: OBAFGKM(LT) mnemonic contest  
win 10 bonus points, and maybe also glamorous prizes

Last time: massive stars—the James Dean of the cosmos

- *live fast*: high mass → strong gravity, high  $T$   
rapidly pass through nuclear burning stages until iron core
- *die young*: in spectacular supernova explosion
- *leave a beautiful corpse*: high-velocity, superheated,  
metal-rich gas ejected, plus compact object at center

## Now that your astro-muscles are strong

You *fully qualify* for upper-level astrophysics **courses**

- ASTR 404: Stellar Astrophysics
- ASTR 405: Solar System and Interstellar Medium
- ASTR 406: Galaxies and the Universe
- ASTR 411: Astronomical Techniques

and you are welcome but *overqualified* for medium-level courses:

- ASTR 330: Extraterrestrial Life
- ASTR 350: Introduction to Cosmology

If you are a LAS Physics major

it's cheap to add **Astronomy Major**

→ many requirements are the same

after ASTR 210: 18 advanced hours, of which  $\geq 10$  from ASTR

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If you are in Engineering, it's cheap to add an **Astronomy Minor**

after ASTR 210: 15 ASTR hours,  $\geq 9$  of which are advanced

## SN 1987A

most recent “nearby” supernova:

Jan. 1987: SN in nearby galaxy (LMC)

www: [discovery image](#)

a lucky “experiment” to test our ideas about supernovae

crown jewel:

★ supernova neutrinos detected on Earth

www: [SuperK](#)

signal as about 20  $\nu$ s, spread over about 10 sec

but came from exploding star 50 kpc = 150,000 lyr away!

www: [2002 Nobel Prize: Masatoshi Koshiba and SuperK](#)

confirms:

- most (> 99%!) of explosion energy carried by  $\nu$ 's
- visible energy only 1% of total!

# Neutron Stars

In supernova core, when collapse begins  
 $e$  degeneracy pressure overcome by removing electrons!  
electrons and protons crushed together

to form forming neutrons and neutrinos:  $p^+ + e^- \rightarrow n + \nu$

- neutrinos escape: star cools by  $\nu$  emission!
- core reaches nuclear density:  $\rho_{\text{nuc}} \sim 10^{18} \text{ kg/m}^3$

neutron star

radius? set by density and mass

$\rho \sim \rho_{\text{nuc}} \sim M/R^3$ , typically,  $M_{\text{NS}} \simeq 1.5M_{\odot}$

$\rightarrow R \sim (M/\rho_{\text{nuc}})^{1/3} \sim 15 - 20 \text{ km}$

tiny! size of Champaign-Urbana!

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*Q: but why doesn't the neutron star itself collapse?*

neutrons, like electrons, are fermions

i.e., obey Pauli principle

→ neutron star supported by degenerate neutrons!

→ a “neutron solid”

...or so theorist imagined

neutron stars originally predicted in mid 1960's

but thought to be so compact that unobservably small

# Pulsars

sources that emit periodic, pulsed radio signals  
discovered accidentally: Jocelyn Bell

www: Princeton pulsar group: audio pulsar

www: 1974 Nobel Prize: Anthony Hewish

Pulsar signals

- periods very regular—better than atomic clocks!
- very fast!  $P$  range 1 s down to  $< 1$  ms!

## A Rotating Star?

*Q: what would happen if Earth spun that fast?*

Warning! If spin too fast  
equator speed  $> v_{\text{esc}} \rightarrow$  unbound!  
equatorial material flung away!

max possible rotation rate at equator:  
when gravity balances centripetal acc.

$$v_c = \sqrt{GM/R}; \text{ but at equator } v_c = 2\pi R/P$$
$$\rightarrow 2\pi R/P = \sqrt{GM/R}$$

$$\text{or } P = 2\pi \sqrt{\frac{R^3}{GM}} = \sqrt{\frac{3\pi}{G\rho}} = \frac{4 \times 10^5 \text{ s}}{\sqrt{\rho}} \quad (\rho \text{ in kg/m}^3) \quad (1)$$

shortest possible period!

density to explain  $P = 1 \text{ ms}$ ?

$$\rho_{\text{min}} \geq (4 \times 10^5 / P)^2 \sim 10^{17} \text{ kg/m}^3$$

$\rightarrow$  must be NS!

Lighthouse Model for Pulsars:

spinning, magnetized NS  $\rightarrow$  beam of radio waves

*diagram: Pulsar spin and off-axis radio beam*

www: Chandra Crab

Note: NS extremely dense  $\rightarrow$  strong gravity

escape speed  $v_{\text{esc}} \sim 1/3 c!$

Newtonian dynamics, gravity:

ok if  $v \ll c$  won't do! need...

www: Big Al



## iClicker Polls: Gravitation Warmup Twofer

Recall your (Newtonian) gravitation

a test particle, mass  $m$ , launched from “infinity” with speed  $v_0 > 0$

passes gravitating mass  $M$

What is the path of the particle?

A no deflection: straight line

B deflected towards  $M$

C deflected away from  $M$

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Same question, but for *massless* test particle,  $m = 0$

## Gravitation Revisited

Newton gravity force law

$$F_{\text{grav}} = \frac{GMm}{r^2} \quad (2)$$

implies that if  $M$  moves and so  $r$  changes:

→ gravity force changes instantaneously over all space!  
“signal” of motion instantaneously transmitted  
throughout the universe

Einstein sez: this is totally illegal! an unmitigated disaster!  
no signal—including gravity—can move faster than  $c$ !

**Einstein's Equivalence Principle:**

in a closed room, no experiment can distinguish  
(non-gravitational) acceleration vs gravity

Q: explain ball drop—Earth's surface vs accelerating rocket?

Rocket Experiment: [www: illuminating animation](http://www.illuminatinganimation.com)

★ light ray deflected

★ entire light path bent (in fact, a parabola!)

But by equivalence principle:

must find same result due to gravity, so:

★ gravity bends light rays

**gravitational lensing**

*Q: what if shine light from basement to attic?*

## Gravitational Redshifting

Also: in accelerating spaceship:

★ shine light from basement to attic

spacecraft & attic speed increases during light travel

→ attic observer sees light *redshifted*

similarly, basement observer sees attic light *blueshifted*

### Gravitational Redshift

And there's more:

redshift = decrease in light frequency  $f$

but  $f = 1/P$ , light wave oscillation period

so redshift →  $P$  increases

but light oscillations are like clock ticking, so...

## Gravitational Time Dilation

- ★ clocks in basement appear to run slow when viewed from attic!  
and attic clocks appear fast when viewed from basement!

in fact, attic clocks faster by  $\Delta t = t_{\text{attic}} - t_{\text{basement}} = g\Delta h/c^2$

- ★ time “warping” due to gravity:  
“**gravitational time dilation**”
- ★ gravity influences “flow” of time!

*Q: how to test these effects in real world?*