

Astro 501: Radiative Processes  
Lecture 37  
April 26, 2013

Announcements:

- **Problem Set 11** last one! *extended* to Wed. May 1
- Please fill out ICES survey! Time is running out!

Last time: 21 cm astrophysics

*Q: what information does it encode?*

*Q: what information does it omit?*

## Awesome Example: Cosmic 21 cm Radiation

radiation transfer along each sightline:

$$T_b = T_{\text{cmb}} e^{-\tau_\nu} + T_{\text{gas}}(1 - e^{-\tau_\nu}) \quad (1)$$

*after gas decoupling, before reionization*  $z_{\text{reion}} \sim 10 \lesssim z \leq z_{\text{dec}}$   
before the first stars and quasars: **cosmic dark ages**  
first structure forming, but not yet “lit up”

during dark ages: intergalactic gas has  $T_{\text{gas}} < T_{\text{cmb}}$

$$\delta T_b \equiv T_b - T_{\text{cmb}} = (T_{\text{gas}} - T_{\text{cmb}})_z (1 - e^{-\tau_\nu})_z \quad (2)$$

we have  $\delta T_b < 0$ : gas seen in 21 cm *absorption*

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*Q: what cosmic matter will be seen this way?*

*Q: what will its structure be in 3-D?*

*Q: how will this structure be encoded in  $\delta T_b$ ?*

# The “21 cm Forest”

what will absorb at 21 cm?

*any neutral hydrogen in the universe!*

but after recomb., most H is neutral, and most baryons are H  
so absorbers are *most of the baryons in the universe*

thus absorber spatial distribution is *3D distribution of baryons*  
i.e., intergalactic baryons as well as seeds of galaxies and stars!  
baryons fall into potentials of dark matter halos, form galaxies  
so *cosmic 21 cm traces formation of structure and galaxies!*

gas at redshift  $z$  absorbs at  $\lambda(z) = (1 + z)\lambda_{\ell u}$

and is responsible for decrement  $\delta T_b[\lambda(z)]$

→ thus  $\delta T_b(\lambda)$  *encodes redshift history* of absorbers

a sort of “21 cm forest”

$\omega$

*Q: what about sky pattern of  $\delta T_b(\lambda)$  at fixed  $\lambda$ ?*

and at fixed  $\lambda$ , sky map of  $\delta T_b(\lambda)$   
gives baryon distribution in “shell” at  $1 + z = \lambda/\lambda_0$   
→ a radial “slice” of the baryonic Universe!

so by scanning through  $\lambda$ , and at each  
making sky maps of  $\delta T_b(\lambda)$   
→ we build in “slices” a *3-D map of cosmic structure evolution!*  
“cosmic tomography”! a cosmological gold mine!  
encodes huge amounts of information

sounds amazing! and it is! but there is a catch!

*Q: why is this measurement very difficult to do?*

⌞ Hint: it hasn't yet been done

## 21 cm Cosmology: The Challenge

The 21 cm cosmic goldmine lies at redshifts  $z \sim 6$  to 150 corresponding to:

- $\lambda_{\text{obs}} \sim 1.5 - 30 \text{ m}$

enormous wavelengths! www: LOFAR

- $\nu_{\text{obs}} \sim 200 - 10 \text{ MHz}$

but ionosphere opaque  $> \nu_{\text{plasma}} \sim 20 \text{ MHz}$

for highest  $z$  (most interesting!) have to go to space! in

fact, have to go to far side of the Moon Q: *why?*

www: proposed lunar observatories

But wait! It's worse!

at these wavelengths, dominant emission is *Galactic synchrotron*

with brightness  $T_{\text{B,synch}} \sim 200 - 2000 \text{ K} \gg T_{\text{cmb}} \gg T_{\text{B,21 cm}}$

www: radio continuum sky

Q: *implications? how to get around this?*

sky intensity  $T_{\text{B,synch}} \sim 200 - 2000 \text{ K} \gg T_{\text{cmb}}$

→ Galactic synchrotron foreground dominates cosmic 21 cm  
curse you, cosmic rays!

But there remains hope!

recall: cosmic-ray electron energy spectrum is a power law

so their *synchrotron spectrum is a power law*

i.e.,  $I_{\nu,\text{synch}}$  is *smooth function of  $\nu$*

compare 21 cm at high- $z$ : a “forest” of absorption lines

not smooth! full of spectral *lines & features*

→ can hope to measure with very good spectral coverage  
and foreground subtraction

- also: can use spatial (i.e., angular) distribution  
e.g., consider effect of first stars (likely massive)  $Q$ : *namely?*

first stars: likely massive → hot → large UV sources  
ionizing photons carve out “bubble” neutral H  
→ corresponding to a *void* in 21 cm  
→ sharp bubble edges may be detectable  
→ 21 cm can probe *epoch of reionization*

hot, ongoing research area!

stay tuned!

# Nebular Diagnostics



# Collisional Excitation

so far we have considered atomic line transitions  
due to emission or absorption of radiation  
but atom *collisions* can also drive transitions

★ collisions can place atoms in excited states  
de-excite radiatively (line emission) → cooling source

★ collisions populate atomic levels  
observing line emission can diagnose density, temperature, radiation field

key physical input: *collision rates*

consider inelastic collisions  $a + c \rightarrow a' + c'$

◦

of species  $a$  with “collision partner”  $c$

*Q: what is collision rate per volume? per  $a$  atom?*

for collisions  $a + c$ , collision rate per volume is

$$\frac{d\mathcal{N}_{\text{collisions}}}{dV dt} \equiv \dot{n}_{ac \rightarrow a'c'} = \langle \sigma_{ac} v \rangle n_a n_c \quad (3)$$

where **collision rate coefficient**  $\langle \sigma_{ac} v \rangle$   
averages over collision *cross section*  $\sigma_{ac}$   
and relative velocity  $v$  between  $a$  and  $c$

*Q: order-of-magnitude estimate for  $\sigma_{ac}$ ?*

*Q: what sets typical  $v$ ?*

collision rate *per a* is

$$\Gamma_{ac \rightarrow a'c'} = \frac{\dot{n}_{ac \rightarrow a'c'}}{n_a} = \langle \sigma_{ac} v \rangle n_c \quad (4)$$

## Two-Level Atom: No Radiation

instructive simple case: a *two-level atom*

denote *ground state* 0, *excited state* 1

with atomic number densities  $n_0$  and  $n_1$

consider effect of collisions with partner  $c$   
when radiation effects are unimportant:

$$\dot{n}_1 = -\Gamma_{10}n_1 + \Gamma_{01}n_0 = -\langle\sigma_{10}v\rangle n_c n_1 + \langle\sigma_{01}v\rangle n_c n_0 \quad (5)$$

Q: what is  $n_1/n_0$  ratio in equilibrium ( $\dot{n}_1 = 0$ )?

Q: what does this imply?

without radiation, in *equilibrium*:

$$\dot{n}_1 == -\langle\sigma_{10}v\rangle n_c n_1 + \langle\sigma_{01}v\rangle n_c n_0 = 0 \quad (6)$$

which gives  $(n_1/n_0)_{\text{eq}} = \langle\sigma_{01}v\rangle / \langle\sigma_{10}v\rangle$

but in *thermal equilibrium*  $(n_1/n_0)_{\text{eq}} = (g_1/g_0) e^{-E_{10}/kT}$

so we have the detailed balance result

$$\langle\sigma_{10}v\rangle = \frac{g_1}{g_0} e^{-E_{10}/kT} \langle\sigma_{01}v\rangle \quad (7)$$

i.e., excitation is suppressed by Boltzmann factor  $e^{-E_{10}/kT}$

*Q: how do we add radiation effects?*

## Two-Level Atom with Radiation

if atoms in excited states exist, they can spontaneously emit  
→ radiation must be present

volume rate of: *spontaneous emission* is  $A_{10}n_1$

volume rate of: *stimulated emission*

$$B_{10}J_\nu n_1 = A_{10} \frac{c^2 J_\nu}{2h\nu^3} n_1 \equiv A_{10} f_\nu n_1 \quad (8)$$

where for isotropic radiation  $J_\nu = 2 \nu^3 / c^2 f_\nu$ , with  $f_\nu$  the *photon distribution function* or occupation number

volume rate of: *true absorption*

$$B_{01}J_\nu n_0 \equiv \frac{g_1}{g_0} A_{10} f_\nu n_1 \quad (9)$$

putting it all together, the two-level atom  
in the presence of collisions and radiation has

$$\dot{n}_1 = \left[ \langle \sigma_{01} v \rangle n_c + f_\nu \frac{g_1}{g_0} A_{10} \right] n_0 - [\langle \sigma_{10} v \rangle n_c + (1 + f_\nu) A_{10}] n_1 \quad (10)$$

this will seek an equilibrium or *steady state*  $\dot{n}_1 = 0$   
giving the ratio

$$\left( \frac{n_1}{n_0} \right)_{\text{eq}} = \frac{\langle \sigma_{01} v \rangle n_c + (g_1/g_0) f_\nu A_{10}}{\langle \sigma_{10} v \rangle n_c + (1 + f_\nu) A_{10}} \quad (11)$$

consider the limits of low- and high-density collision partners

$$\left( \frac{n_1}{n_0} \right)_{\text{eq}} \rightarrow \begin{cases} (g_1/g_0) f_\nu / (1 + f_\nu) , & n_c \rightarrow 0 \\ \langle \sigma_{01} v \rangle / \langle \sigma_{10} v \rangle & n_c \rightarrow \infty \end{cases} \quad (12)$$

*Q: implications of limits if  $T_{\text{rad}} \neq T_{\text{gas}}$ ?*

in steady state:

$$\left(\frac{n_1}{n_0}\right)_{\text{eq}} = \frac{\langle\sigma_{01}v\rangle n_c + f_\nu(g_1/g_0)A_{10}}{\langle\sigma_{10}v\rangle n_c + (1 + f_\nu)A_{10}} \quad (13)$$

at *low density* of collision partners:  $n_c \rightarrow 0$  and thus

$$\left(\frac{n_1}{n_0}\right)_{\text{eq}} \rightarrow \frac{g_1}{g_0} \frac{f_\nu}{1 + f_\nu} \stackrel{\text{therm}}{=} \frac{g_1}{g_0} e^{-E_{10}/kT_{\text{rad}}} \quad (14)$$

→ *level population set by radiation temperature*  $T_{\text{rad}}$

at *high density* of collision partners:  $n_c \rightarrow \infty$ , and

$$\left(\frac{n_1}{n_0}\right)_{\text{eq}} \rightarrow \frac{\langle\sigma_{01}v\rangle}{\langle\sigma_{10}v\rangle} = \frac{g_1}{g_0} e^{-E_{10}/kT_{\text{gas}}} \quad (15)$$

→ *level population set by gas temperature*  $T_{\text{gas}}$

Q: characteristic density scale?

## Critical Density

for each collision partner  $c$ , excited state de-excitation by emission and by collisions are equal when

$$\langle \sigma_{10} v \rangle n_c = (1 + f_\nu) A_{10} \quad (16)$$

this defines a **critical density**

$$n_{c,\text{crit}} = \frac{(1 + f_\nu) A_{10}}{\langle \sigma_{10} v \rangle} \quad (17)$$

- if  $f_\nu \ll 1$ : stimulated emission not important (PS11)  
 $n_{c,\text{crit}} \rightarrow A_{10} / \langle \sigma_{10} v \rangle$  depends only on  $T$  and atomic properties
- but if  $f_\nu$  not small, critical density depends on local radiation field

so when partner density  $n_c \gg n_{c,\text{crit}}$ :

state population set by  $T \rightarrow T_{\text{gas}}$

and when  $n_c \ll n_{c,\text{crit}}$ :

state population set by  $T \rightarrow T_{\text{rad}}$