

Astro 210
Lecture 5
Jan 26, 2018

Announcements

- HW1 due today at 5pm
- HW2 available; due in 1 week
- **register** your iClicker; link on course webpage
- first Planetarium shows Mon Feb 5 and Wed Feb 7
info online: **reservations**, schedules, directions, report form
- if this is your first class: see me afterward!

Last time: planets

- paths on celestial sphere are (nearly) great circles
stay near ecliptic, in zodiac *Q: and so?*
- motion: mostly eastward w.r.t. celestial sphere, like Sun, Moon
- but sometimes *retrograde* *Q: what's that?*
- retrograde occurrence related to planet angle from Sun *Q: how?*

Today: building scientific models to explain naked-eye sky

Cosmological Models: Naked-Eye Sky

any viable model must *explain all observations*
including retrograde motion of planets

models change:

- when predictions fail
- when new observations require new explanations

model refined → **theory**

theory is *end product* of model \leftrightarrow data

not mere speculation or offhand/wacky idea

Greek Cosmology

Pythagoreans

outlook: geometry is everything, perfected in spheres

- earth: spherical shape

observations of Eratosthenes (276-195 BC)

altitude of noonday Sun at solstice:

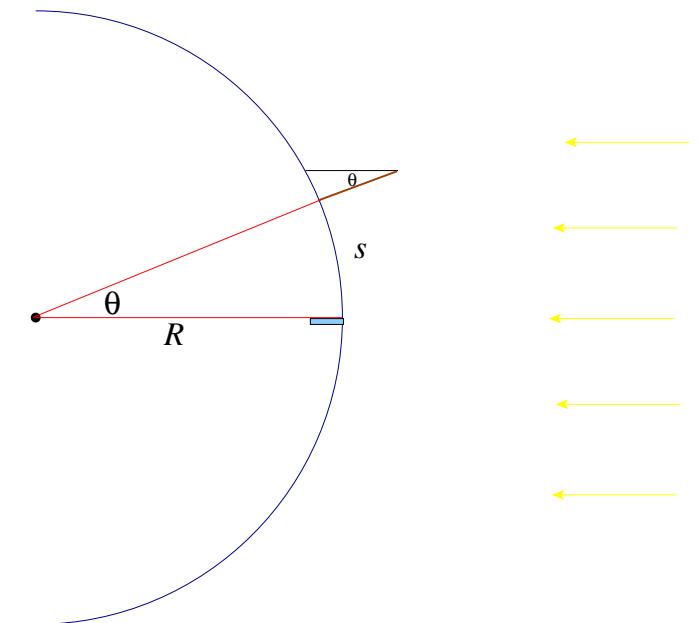
- directly overhead at Syene, Egypt
 $\theta = 7^\circ$ from vertical at Alexandria

Q: what do we learn from the simple fact that the angles differ?

- pace off distance $s \sim 800$ km

geometry: $s/R = \theta_{\text{radians}} = 2\pi(7^\circ/360^\circ)$

$\Rightarrow R \sim 6700$ km: close!



4

- Moon, Sun, planets, stars fixed on spheres which move in uniform circular motion

Geocentrism

Ancient Greeks: Earth is center of universe (“geocentric”)

- ★ rise & set of sun/moon/planets can be explained Q: *how?*
- ★ we don’t *feel* Earth is spinning
 - would mean we move at 900 mph w.r.t. Earth center
 - why aren’t we flung off?
- ★ apparent lack of **stellar parallax**

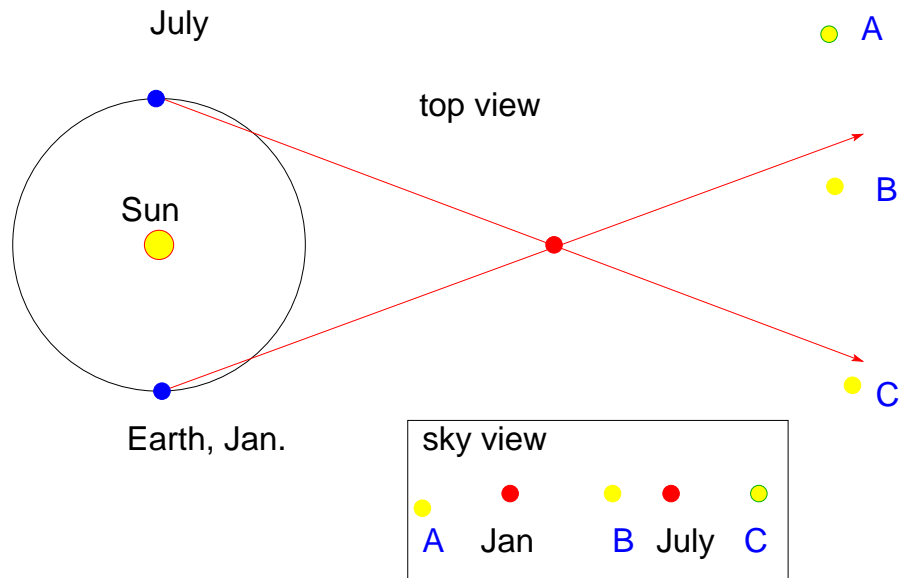
Proof by contradiction: *what if* earth orbits sun?

Consider view of stars from moving Earth

Q: *diagram?*

Stellar Parallax: Take One

if earth moves \rightarrow star positions change on celestial sphere



foreground star should appear to *shift* w.r.t. background stars

but parallax effect *not* observed!

o

Q: *why?*

Q: *if you are Aristotle, what do you conclude?*

Why no parallax?

eye cannot resolve angles $\lesssim 1' = 1 \text{ arc min} = 60 \text{ arc sec}$
turns out—typical shift on sky: $\sim 1'' = 1 \text{ arc sec}$ – very small effect!

parallax not detected until $\sim 1830(!)$

Aristotle explained data available at the time
and gave strong evidence **against** Sun-centered picture!

iClicker Poll: The Geocentric Celestial Sphere

Consider the geocentric picture of Aristotle and Ptolemy, in which the celestial sphere is literally a sphere.

What is the motion of this sphere?

- A no motion; at rest
- B uniform rotation with period = 1 year
- C uniform rotation with period = 1 day
- D nonuniform rotation, period = 1 year, precession by $\pm 23.5^\circ$

∞

*Q: What does the geocentric model (described thus far) explain?
what not?*

Geocentric Grunge

must explain **Retrograde motion**
cannot do this with circular orbits
(having constant angular velocity)

solution must complicate the orbit:
add deferent and **epicycle**

www: epicycle animation

Claudius Ptolemy ~ 125 AD

Constructed complete geocentric model
every planet had epicycles—in fact, epicycles on top of epicycles
complicated/elaborate model, but also sophisticated

Ptolemy accounted for

- non-uniform angular speed
- retrograde motion
- because Mercury and Venus *never* seen in opposition
center of their epicycles placed on line
connecting earth and sun

how good: observations decide!

☞ Errors generally < 5 deg: not bad but observable!
remained in use for ~1400 years!!

iClicker Poll: Ptolemy & Science

Vote your conscience!

Is Ptolemy's system a scientific model for the naked-eye sky?

A

yes

B

no

A Cosmological Revolution

we fast forward 1.5 millenia → Renaissance Europe
the age of da Vinci, Michelangelo, Elisabeth I, Shakespeare
...and:

Nicolaus Copernicus 1473–1543 Polish

offended by Ptolemy's system (on esthetic grounds: “ugly”)
adopted **heliocentric** (Sun-centered) cosmological model

Copernican Model

- *Earth spins* ⇒ daily motion of celestial objects
- *Earth orbits Sun* ⇒ apparent Sun motion in zodiac
- Mercury & Venus orbits inside Earth's ⇒ always seen near Sun
- retrograde motion: naturally caused by Earth–planet passing

www: animation

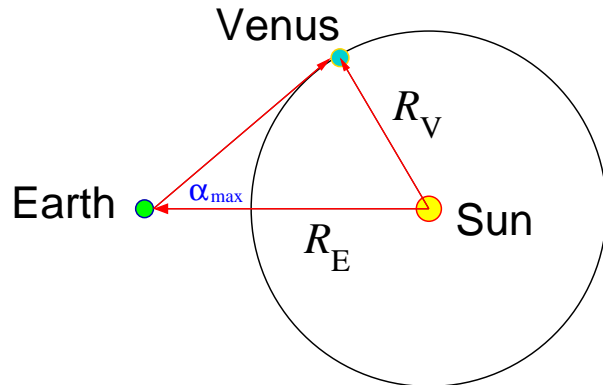
simply explains retrograde correlations w/ planet location

- lack of stellar parallax ⇒ must assume large distance to stars

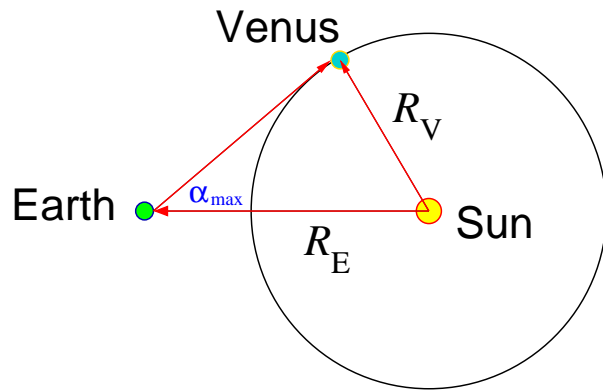
Copernicus and Distances

Copernicus model also allowed him to calculate *relative distances* of planets

Venus: maximum angle (max “elongation”) from Sun observed as $\alpha_{\max} = 46^\circ$



- 13 Q: max elongation geometry in heliocentric model?
Q: that is, what's special about this triangle?



from diagram: right triangle, Earth-Sun distance is hypotenuse

$$\Rightarrow \sin \alpha_{\max} = R_V / R_E$$

$$\Rightarrow R_V = R_E / \sin \alpha_{\max} = 0.72 R_E$$

New unit: “astronomical unit” = average Earth-Sun distance

$$1 \text{ AU} \equiv R_E = 1.50 \times 10^8 \text{ km}$$

- Earth (average) orbit radius: 1 AU
- Venus orbit: 0.72 AU